Fundamentals of Traffic Operations and Control

Actuated Traffic Signal Design

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Outline

- Introduction
- Problem description / Terminology
- Classification of control strategies
 - Fixed-time control
 - Traffic actuated control
 - Traffic responsive control
 - Adaptive control
- Discussion



Introduction

Original reason for traffic lights:

safe crossing of antagonistic streams of vehicles and pedestrians

- Once they exist, they can be set in different ways:
 optimization problem
- Difficulties:

binary variables, large dimensions, many disturbances, available measurements, real-time constraints

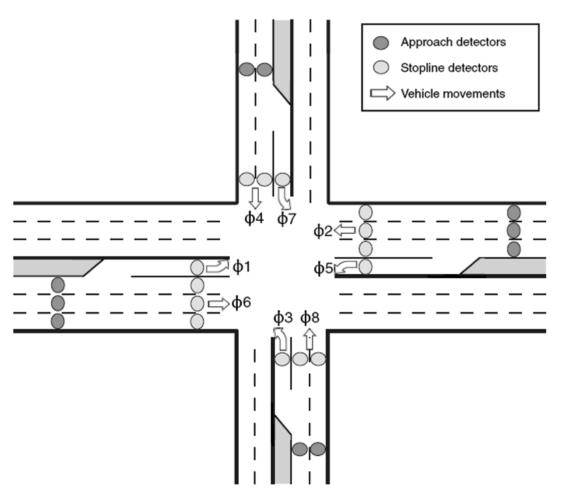
Many control strategies:

both heuristic and systematic



Terminology

junction (UK); intersection (US)



Each vehicle movement has an associated phase number.

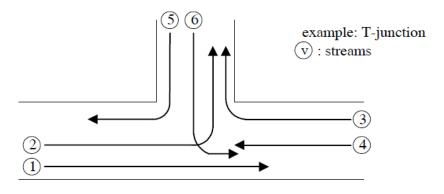
Phases have approach detectors and/or stopline detectors.

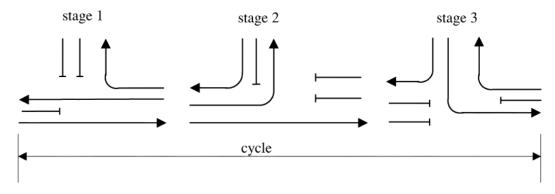
Stage: set of compatible phases.

Signal cycle: one repetition of all signals.

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Example: T-junction





Isolated intersection control

Fixed-time (pre-timed)

Time-of-Day

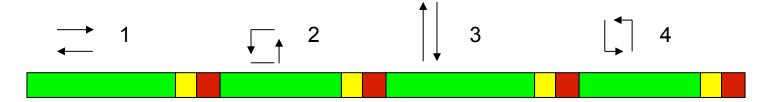
Actuated

- Semi-actuated
- Fully-actuated

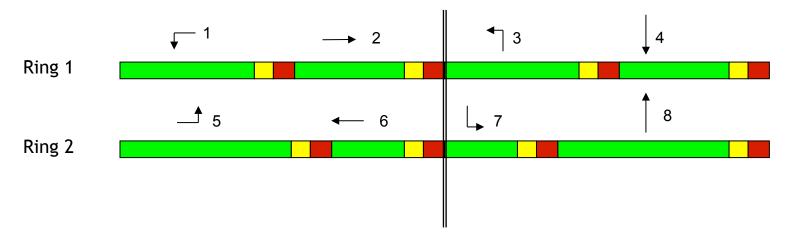


Modelling a plan with rings

Single ring controller



Dual ring controller



Permitted/Protected left turns.



Actuated control

Vehicle actuations change the phases durations (and cycle length).

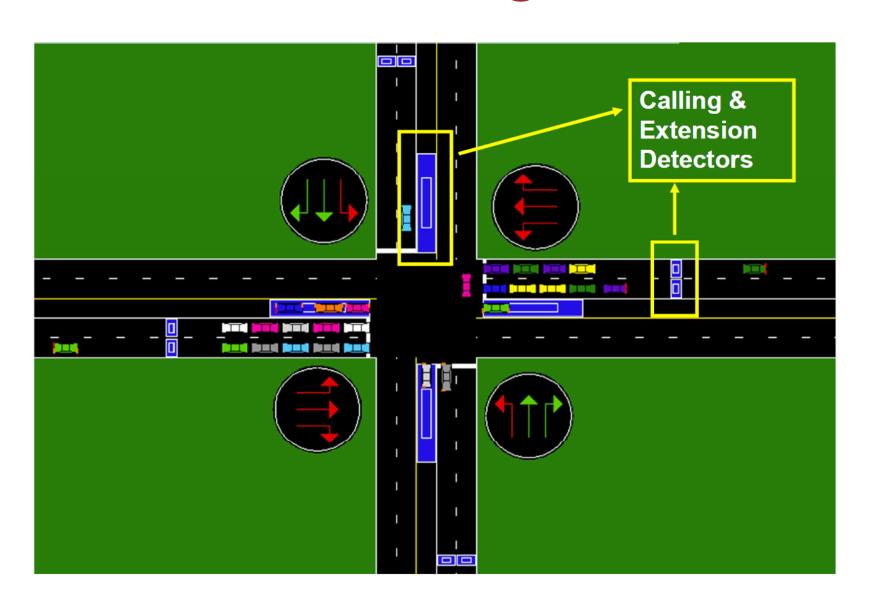
Min, max greens (pedestrians).

Phase skip; gap acceptance; recall.

- Semi-actuated (coordination)
- Fully-actuated (change cycles)

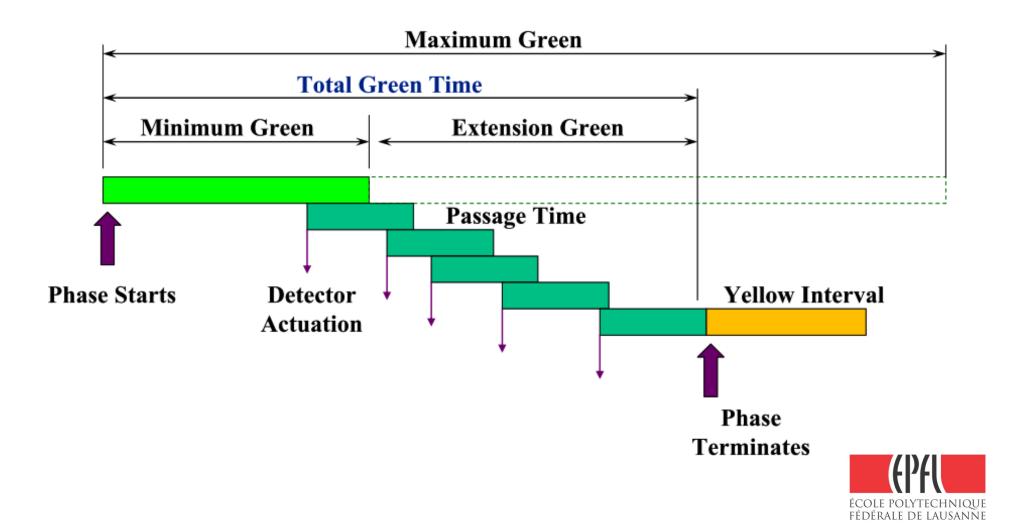


Traffic actuated signal control



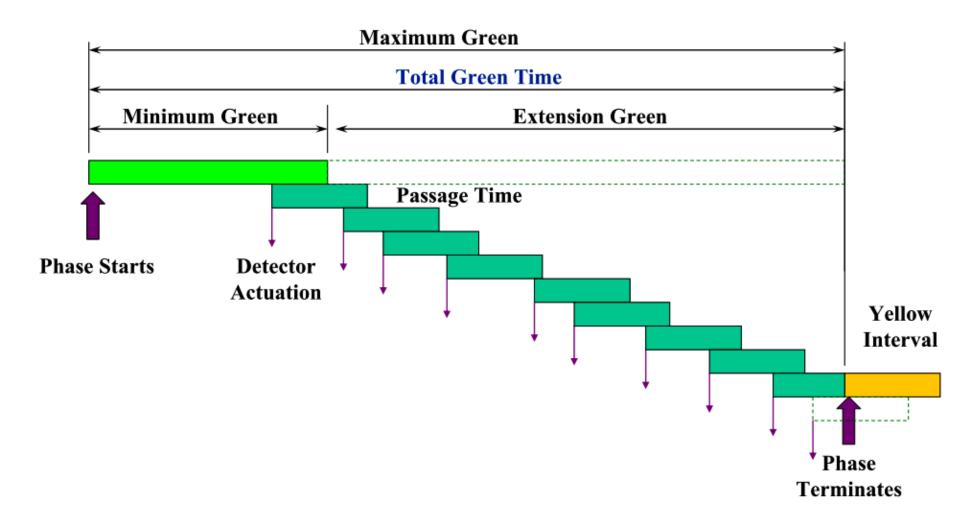
Operation of an actuated phase

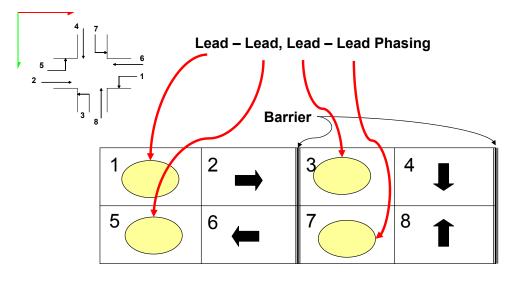
Case 1: Max green not reached (Gap out).

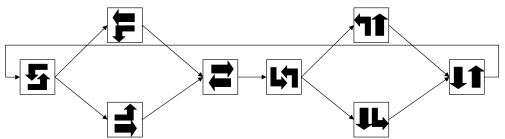


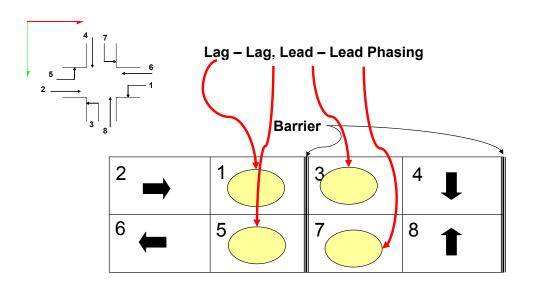
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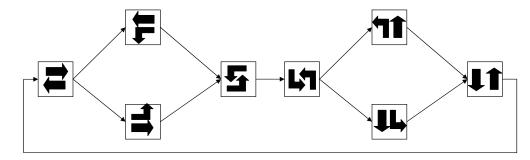
Case 2: Max green reached (Max out).

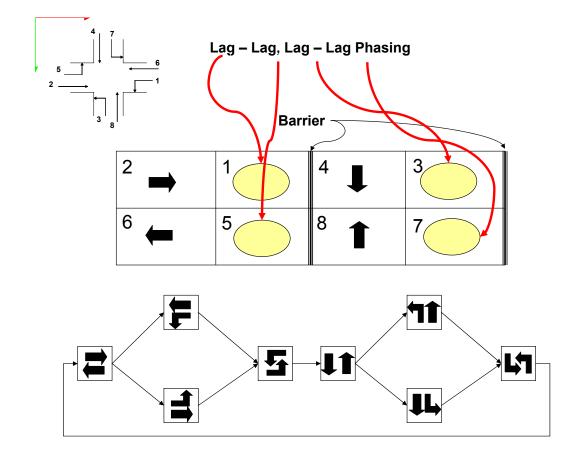


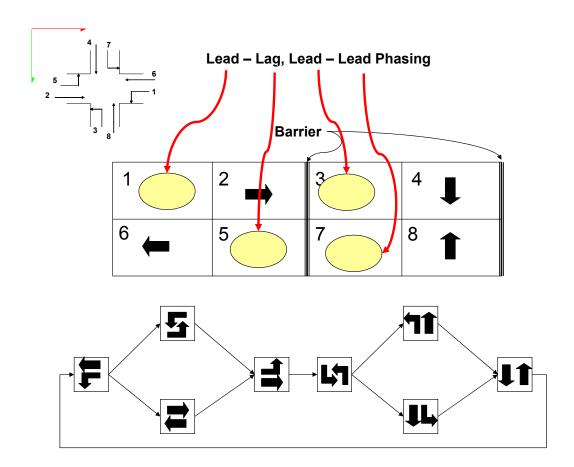


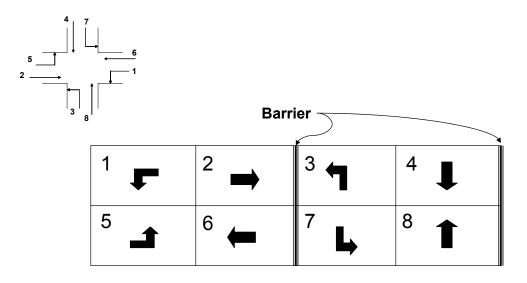


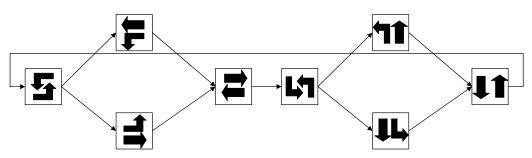


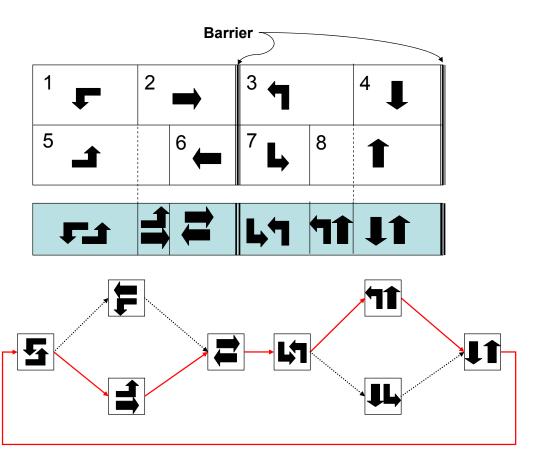


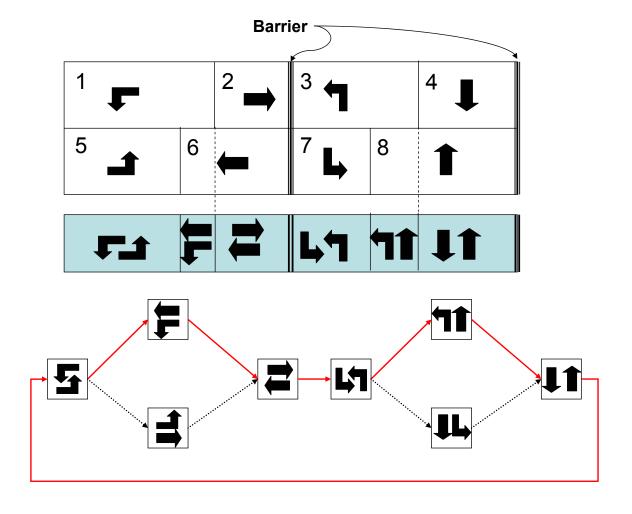


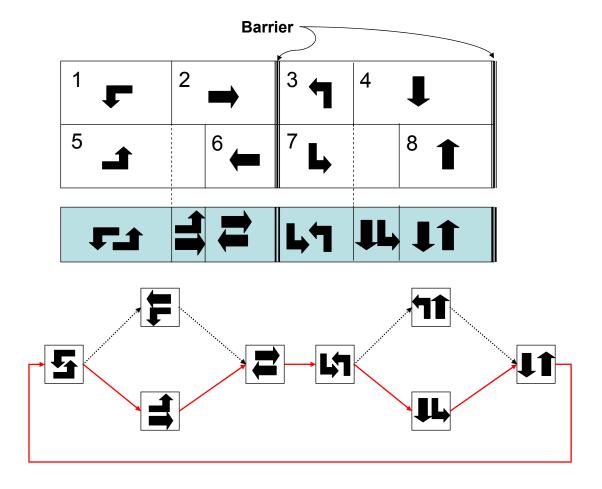


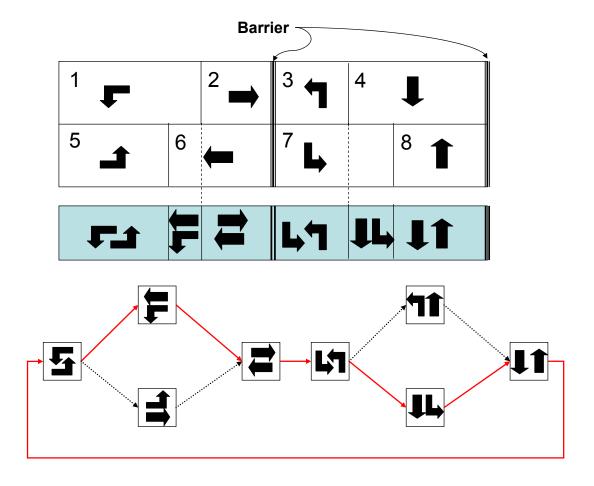












Adaptive signal control

More sophisticated algorithms:

- include internal models for dynamics and optimization
- compute signal parameters including splits, cycles, offsets in real-time based on measurements



Adaptive strategies

Many strategies (research or commercial):

SCOOT

SCATS

OPAC

PRODYN

CRONOS

RHODES

UTOPIA

BALANCE

TUC

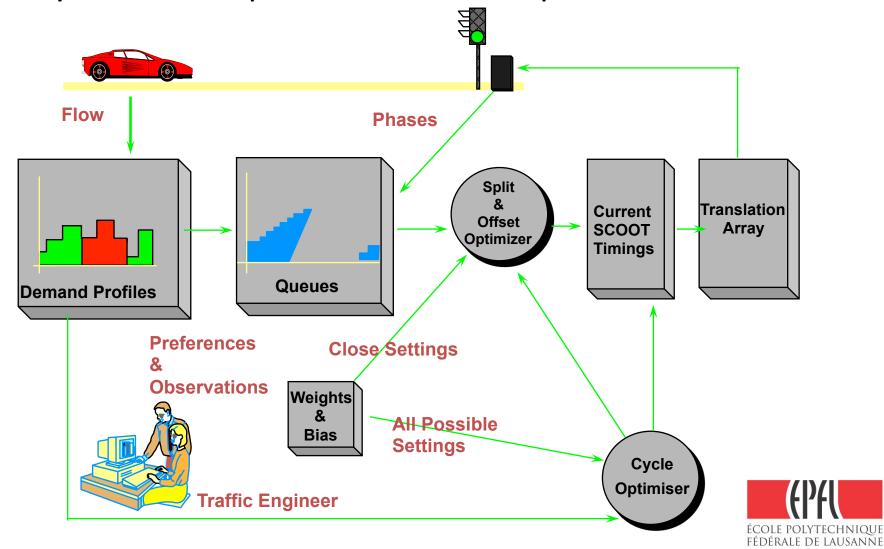
ACS-Lite

Examples are provided for general knowledge of the students. It will not be taught inside classroom.

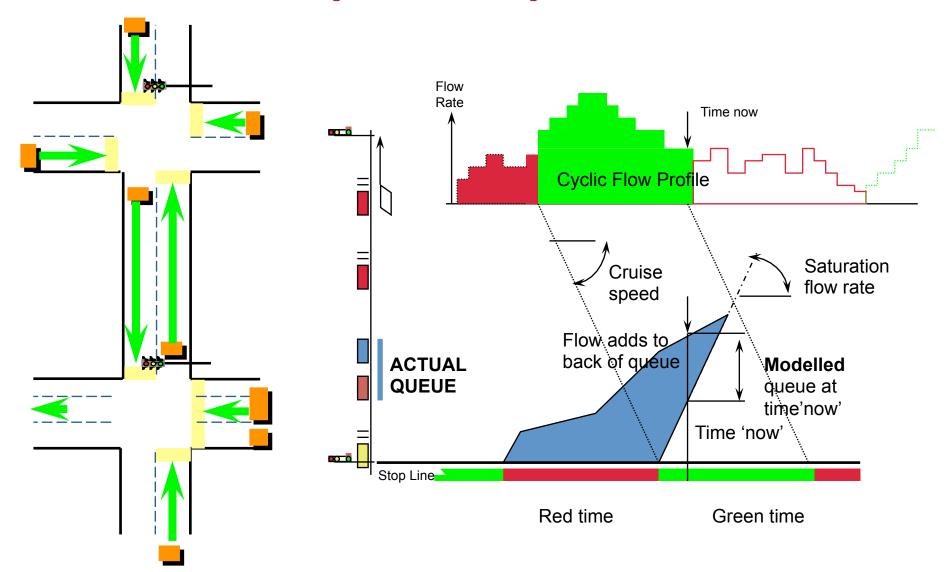


SCOOT - UK

Split Cycle Offset Optimization Technique:



SCOOT – Loop detectors position, demand profile, queue model



Signal optimizers

Optimizer	Frequency	Change time (seconds)
Split	Every stage	-4, 0, +4 (temporary) -1, 0, +1 (permanent)
Cycle	Once per cycle	-4, 0, +4
Offset	Every 2.5 or 5 minutes	-4, 0, +4 (32 to 64) -8, 0, +8 (64 to 128) -16, 0, +16 (128 to 240)

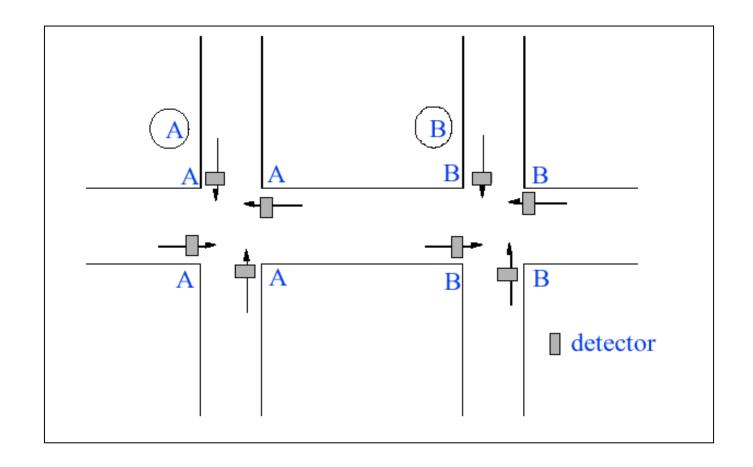
SCATS – Australia

Sydney Coordinated Adaptive Traffic System:

Objectives:

- Minimize stops (light traffic).
- Minimize delay (heavy traffic).
- Minimize travel time.
- Stopline detection.
- Network divided into regions.
- Each region divided into links and nodes.
- For each region calculate degree of saturation (DS) for all nodes.

SCATS – Stopline detection



Degree of saturation: DS = [green-(unused green)]/green

SCATS – Optimization

Cycle Length (CL):

- User defined equilibrium DS values are used to determine the relationships between measured DS and CL.
- The relationships are used to select a target CL toward which the actual CL moves.

Offsets:

- Offset plans are selected by comparing traffic flows on the links.
- The weighted three-cycle average volumes are used for each candidate offset.

SCOOT vs. SCATS

- Model
- Central control
- Upstream detection
- Fixed traffic region

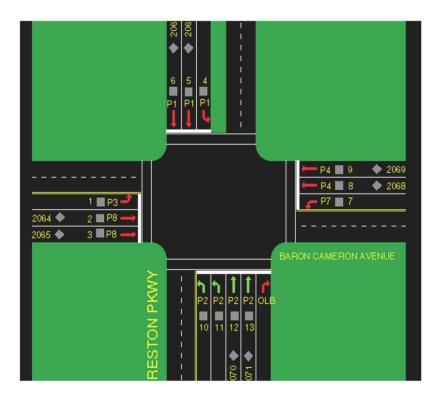
- Algorithm
- Distributed
- Stop-line detection
- Adjustable regions

- Closed systems: not all the details are known.
- Involvement of many (implementation specific) heuristics.



OPAC/RHODES: no fixed cycle

- Measured and predicted vehicle arrivals
- Optimization: minimize queues
- Rolling horizon



- Upstream detectors can provide history for demand profiles.
- Smoothed volume can be used for uniform profiles.

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 Platoon identification and smoothing can be used for cyclic profiles.

Adaptive Traffic Signal Control: Principles and Applications of Max-Pressure

Jack Haddad

Fundamentals of Traffic Operations and Control (CIVIL-457)



Introduction Background Fixed cyclic MP Dynamic cyclic MP Simulation results Experimental study Conclusions

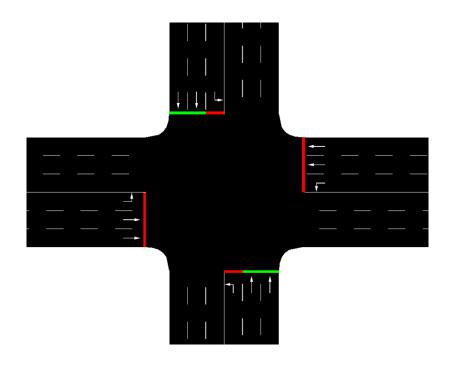
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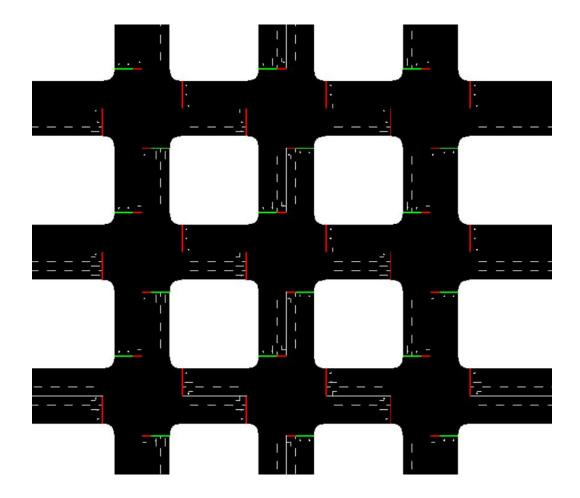
Large scale urban traffic networks

- Transportation systems play a vital role in ensuring the economic growth and sustainable development of society.
- Poor traffic management could lead to environmental and economical damages due to congestion.
- Traffic signal is one of the main measures of traffic management.
- As the network size increases the complexity of the problem increases.

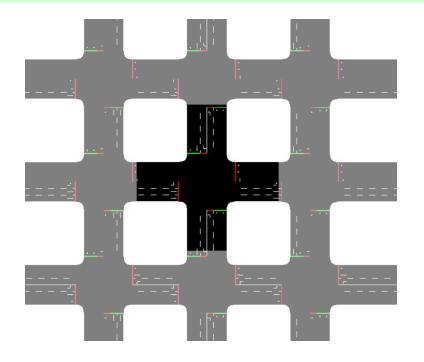


Large scale urban traffic networks

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- As the network size increases the complexity of the problem increases.



Hence, distributed approaches can provide promising solutions.



Problem formulation - Dynamic cycle time in traffic signal of cyclic max-pressure control

Given:

- \hookrightarrow travel times of all links (or movements) considered

Determine:

 \hookrightarrow green time durations for all phases at all intersections

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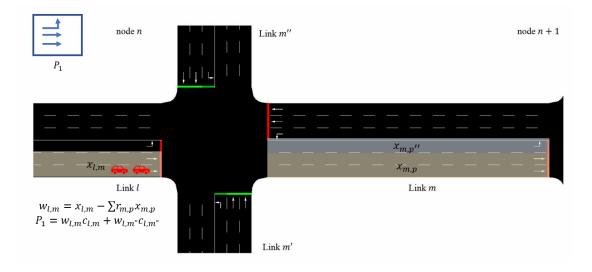
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Original Max-Pressure algorithm (Varaiya 2013)

- Was initially proposed for scheduling packets in wireless communication networks.
- A distributed algorithm that maximizes throughput while stabilizing the queues.
- Algorithm inputs: queues, turn ratios, control plan (phases).
- Pressure: the difference between the upstream and the (average) downstream queue lengths.



The original Max-Pressure traffic controller based on queue lengths (MP-QL)

The MP control policy $u^*(t): x \to s$, actuates the maximum pressured phase each time step t at each intersection:

$$u^*(t) = \operatorname{argmax} \{ P_s(t) | s \in S_n \}, \tag{1}$$

 S_n – set of all phases of intersection n.

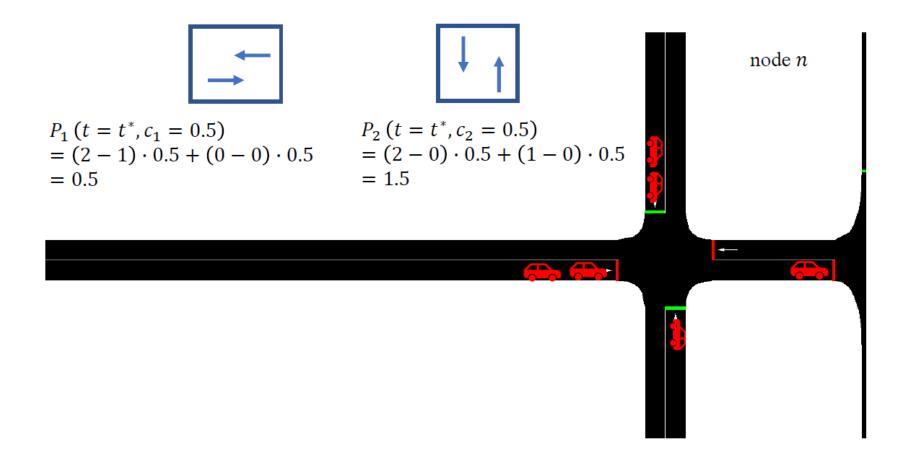
The pressure of phase s at intersection n is calculated as:

$$P_{s}(t) = \sum_{(l,m)} w_{l,m}(t)c_{l,m}(t)s_{l,m}(t)$$

$$= \sum_{(l,m):s_{l,m}=1} w_{l,m}(t)c_{l,m}(t), \quad \forall s \in S_{n}.$$
(2)

$$w_{l,m}(t) = x_{l,m}(t) - \sum_{p} r_{m,p}(t) x_{m,p}(t), \quad \forall m \in \text{Out}_n, \, \forall l \in \text{In}_n, \, \forall p \in \text{Out}_{n+1}.$$
 (3)

Original Max-Pressure traffic controller (MP-QL)



Since then several MP algorithms were developed...

- queue-based vs. time-based
 - Most previous MP algorithm controllers are queue-based feedback.
 - One real application was performed on time-based MP in *Mercader et al. 2020*.
- signal update: every time step vs. every cycle
- features:
 - infinite vs. finite link capacity
 - non-fixed phase sequence (acyclic) vs cyclic
 - stability vs. work conservative
 - phase switching gap (lost time)
 - ...

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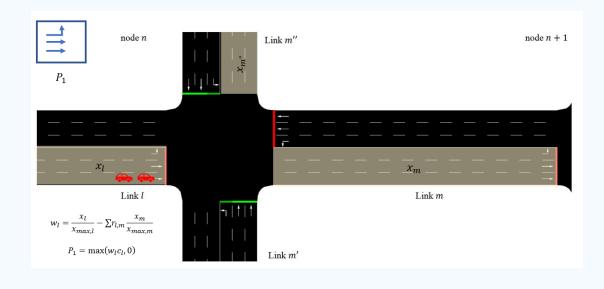
A modified cyclic Max-Pressure traffic controller based on queue lengths (MP-QL) - Kouvelas et al. 2014

Pressures:

$$P_{s,n}(t) = \max\left(0, \sum_{(I,m)\in s} w_I(t)c_I(t)\right), \qquad \forall I \in \mathbf{In}_n, \quad s \in \mathbf{S}_n$$
 (4)

Weights:

$$w_{l}(t) = \frac{x_{l}(t)}{x_{\text{max},l}} - \sum_{m} r_{l,m} \frac{x_{m}(t)}{x_{\text{max},m}}, \quad \forall m \in \text{Out}_{n}, \quad \forall l \in \text{In}_{n}$$
 (5)



A modified cyclic Max-Pressure traffic controller based on queue lengths (MP-QL) - Kouvelas et al. 2014

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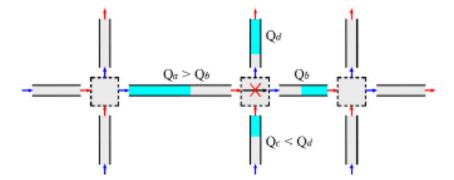
Green allocations for each phase included in each cycle time:

$$G_n = C_n - L_{\text{lost},n} - \sum_s g_{\min,s,n} , \qquad \forall s \in S_n ,$$
 (6)

$$g_{s,n}(t) = \frac{P_{s,n}(t)}{\sum_{s} P_{s,n}(t)} G_n + g_{\min,s,n}.$$
 (7)

Queue based Max-Pressure traffic controller (MP-QL) limitations

- The MP controller in *Kouvelas et al. 2014* considers the queue lengths at *links*, thus being mainly efficient at intersections with link-based phases.
- The spatial distribution of the queues is neglected (*Li and Jabari (2019)*).



• Impractical, due to inefficient online data collection in the real world.

Real implementation (May 30, 2018)



Mercader, Uwayid, and Haddad 2020 (TR-C)

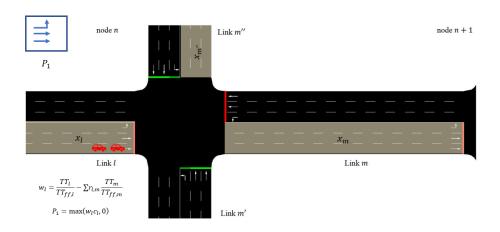
 MP controller based on travel times (TT) achieves better performance than the historic performance delivered by the optimized fixed control used at the intersection.

The cyclic Max-Pressure traffic controller based on Average Travel Time (MP-TT) - Mercader et al. 2020

- is a cycle-step algorithm with link structure,
- it shares the same equations of queue length based MP controller (MP-QL) in Kouvalas 2014,

$$w_{l}(t) = \frac{TT_{l}(t)}{TT_{ff,l}} - \sum_{m} r_{l,m} \frac{TT_{m}(t)}{TT_{ff,m}}, \quad \forall m \in \text{Out}_{n}, l \in \text{In}_{n},$$
(8)

 $TT_I(t)$ [s] – average travel time during the cycle t at the link I, $TT_{ff,I}$ [s] – travel time in free flow at link I.



Time based MP limitations (in Mercader et al. 2020):

- The MP-TT controller uses a link-based approach (similar to Kouvelas et al. 2014).
- It applies conversion from normalized queues to normalized travel times as if the relation is linear $\frac{x_l(t)}{x_{\max,l}} \sim \frac{TT_l(t)}{TT_{ff,l}}$, which is not necessarily the case.

Time based MP limitations (in Mercader et al. 2020):

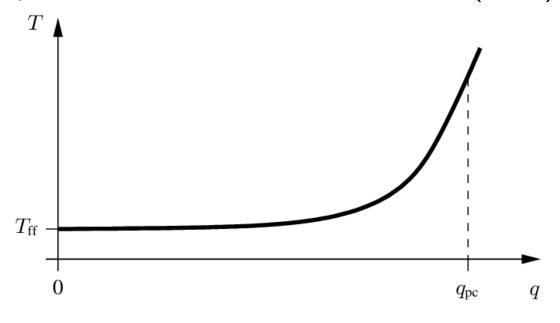
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Contributions... Improved cyclic time based MP controller:

- (C1) Enhanced relation of the queue normalization with travel time (delays),
- (C2) Improved generic algorithm that can be applied over a larger variety of intersections (heterogeneous networks, lane based).

(C1) Average Travel Time (MP-TT) \Rightarrow Travel Time Delays (MP-TTD)

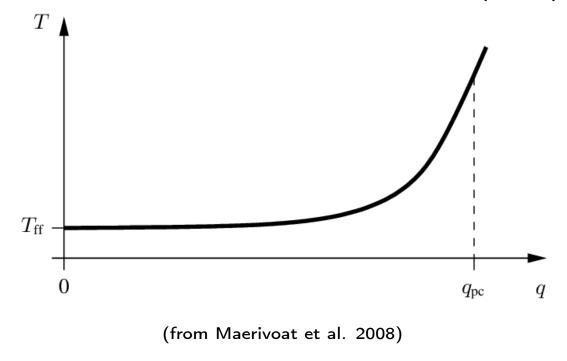
Inspired from Bureau of Public Roads (1964)



(from Maerivoat et al. 2008)

(C1) Average Travel Time (MP-TT) ⇒ Travel Time Delays (MP-TTD)

Inspired from Bureau of Public Roads (1964)



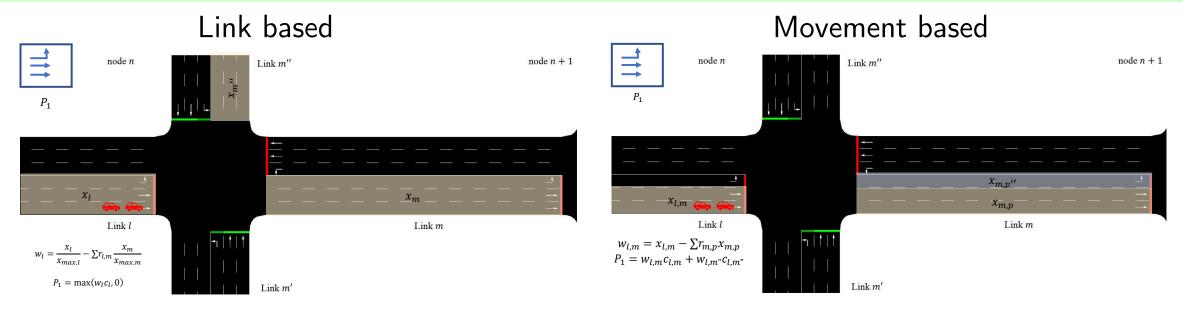
$$TT = TT_{ff} \left[1 + \alpha \left(\frac{x}{x_{max}} \right)^{\beta} \right]$$

It is used to support the convex relationship between the normalized travel time and the normalized queue length,

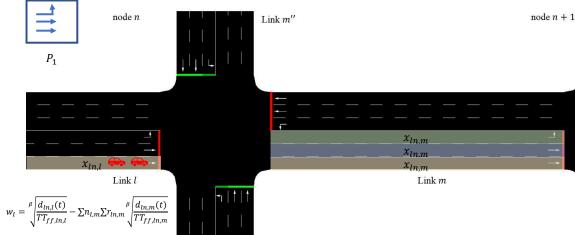
$$\sqrt[\beta]{\frac{TT - TT_{ff}}{TT_{ff}}} \sim \frac{x}{x_{\text{max}}} \tag{9}$$

 β – a fitting parameter to the nonlinearity relation.

(C2) Improved generic algorithm (heterogeneous networks, lane based)



Lane based



Travel time delays based MP traffic controller (MP-TTD)

The new suggested equations for the pressures and weights are,

$$P_{s,n}(t) = \max\left(0, \sum_{ln \in s} w_{ln}(t)c_{ln}(t)\right), \quad \forall s \in S_n$$
(10)

$$w_{ln}(t) = \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\mathrm{ff},ln}}} - \sum_{m} n_{l,m}(t) \sum_{ln \in m} r_{ln,m}(t) \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\mathrm{ff},ln}}}$$

$$\forall ln \in s, m \in \operatorname{Out}_{ln,n}, l \in \operatorname{In}_n,$$
 (11)

where

$$d_{ln}(t) = \max(TT_{ln}(t) - TT_{ff,ln}, 0), \qquad (12)$$

$$r_{ln,m}(t) = \sum_{p} \frac{r_{m,p}(t)}{N_{m,p}}, \quad \forall m \in \operatorname{In}_{n+1}, \ p \in \operatorname{Out}_{ln,n+1},$$
 (13)

Green allocations with fixed cycle: (similar to Mercader et al. 2020, Kouvelas et al. 2014)

$$G_n = C_n - L_{\text{lost},n} - \sum_s g_{\min,s,n}$$
, $\forall s \in S_n$, (14)

$$g_{s,n}(t) = \frac{P_{s,n}(t)}{\sum_{s} P_{s,n}(t)} G_n + g_{\min,s,n}.$$
 (15)

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Dynamic cyclic structure of MP algorithm

Problem

Previous works of cyclic-based MP control have offered a cyclic notion to actuate the controller in a cyclic manner. Yet no input has been provided for

- optimal cycle length for each intersection,
- offset problem: in a grid network structure along with the dynamic and stochastic nature of the trips, it is not clear what the main phase of the intersections and how to coordinate them.

Dynamic cyclic structure of MP algorithm

Motivation

- developing two dynamic cyclic schemes (bounded and unbounded cycle lengths) with low computational complexity,
- evaluating the developed control schemes via comparing traffic performances from simulation results between dynamic and fixed cycle lengths.

Fixed Cycle

- Fixed phase sequence (cannot skip phases)
- A fixed cycle is determined a priori, and is equal in consecutive intersections
- Green allocations are updated each cycle time

Dynamic Cycle

- Fixed phase sequence (cannot skip phases)
- The phase actuation is updated each time step
- If the activated phase holds the maximum pressure it is re-activated another time step, else, the next phase in the sequence is activated

Travel time delays based MP traffic controller (MP-TTD)

The new suggested equations for the pressures and weights are,

$$P_{s,n}(t) = \sum_{ln \in s} w_{ln}(t)c_{ln}(t), \quad \forall s \in S_n$$
(16)

$$w_{ln}(t) = \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\mathrm{ff},ln}}} - \sum_{m} n_{l,m}(t) \sum_{ln \in m} r_{ln,m}(t) \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\mathrm{ff},ln}}}$$

$$\forall In \in s, \ m \in \operatorname{Out}_{In,n}, \ I \in \operatorname{In}_n, \tag{17}$$

where

$$d_{ln}(t) = \max(TT_{ln}(t) - TT_{ff,ln}, 0), \qquad (18)$$

$$r_{ln,m}(t) = \sum_{p} \frac{r_{m,p}(t)}{N_{m,p}}, \quad \forall m \in \operatorname{In}_{n+1}, \ p \in \operatorname{Out}_{ln,n+1},$$
(19)

Dynamic cyclic structure of MP algorithm - Unbounded length

```
Algorithm 1 Dynamic Cyclic Max-Pressure - Unbounded
 1: procedure DYNAMICCYCLEMP(g_{S_n,\min}, S_n, s_{i,n}, t) #Cycle fixed sequence should be determined
         if t < g_{s_{i,n},\min} then
              t \leftarrow t + 1
         else
             t \leftarrow 0
              # Calculate the weights and the pressure based on the MP-controller
             w_{ln}(t) \leftarrow \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\text{ff},ln}}} - \sum_{m} n_{l,m}(t) \sum_{ln \in m} r_{ln,m}(t) \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\text{ff},ln}}}
              P_{s_{i,n}}(t) \leftarrow \sum_{ln \in s_{i,n}} w_{ln}(t) c_{ln}(t)
              if s_{i,n} = \arg\max_i(P_{s_{i,n}}) then
                  return s_{i,n} #Actuate the same phase again
10:
              else
11:
                  return s_{i+1,n} #Actuate the next phase in the sequence
12:
              end if
13:
         end if
14:
15: end procedure
```

Dynamic cyclic structure of MP algorithm - Bounded length

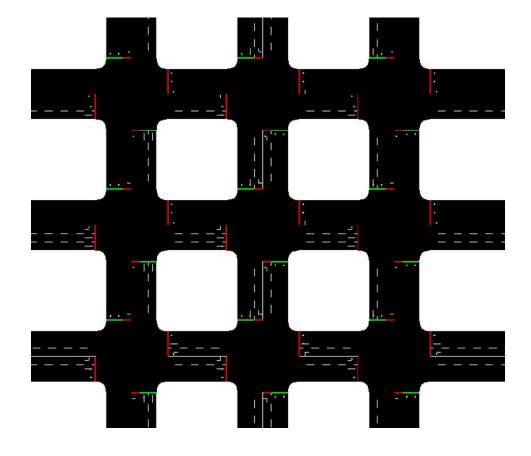
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Algorithm 2 Dynamic Cyclic Max-Pressure - Bounded
 1: procedure DYNAMICCYCLEMP(maxCycle, g_{S_n, min}, S_n, s_{i,n}, t, m) #Cycle fixed sequence should be
    determined, m - number of phase activation within the cycle, e.g. m=1 is the first phase activated in
    a cycle.
        if t < g_{s_{i,n},\min} then
             t \leftarrow t + 1 for
        else
             t \leftarrow 0
             m \leftarrow m + 1
             # calculate maximum times phase i can be activated in a single cycle (a cycle with bounded
    length)
            maxNumber_{S_{0,n}} \leftarrow (maxCycle - L - \sum_{j=1}^{length(S_n)} g_{s_{i,n},min})/g_{s_{0,n},min}
             for i in length(S_n) - 1 do
                 maxNumber_{S_{j+1,n}} \leftarrow 1 + (maxNumber_{S_{j,n}} - m) \frac{g_{s_{i,n},\min}}{g_{s_{i+1,n},\min}} + m \#  If the phases share the
    same minimum green then this equation would be static, maxNumber_{S_{i+1,n}} \leftarrow 1 + maxNumber_{S_{i,n}}
             end for
11:
             # Calculate the weights and the pressure based on the MP-controller
             w_{ln}(t) \leftarrow \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\text{ff},ln}}} - \sum_{m} n_{l,m}(t) \sum_{ln \in m} r_{ln,m}(t) \sqrt[\beta]{\frac{d_{ln}(t)}{TT_{\text{ff},ln}}}
             P_{s_{i,n}}(t) \leftarrow \sum_{ln \in s_{i,n}} w_{ln}(t) c_{ln}(t)
14:
             if s_{i,n} = \arg \max_{s}(P_{s_{i,n}}) and m < \max Number_{S_{i,n}} then
15:
                 return S_{i,n} and m #Actuate the same phase again and return the phase number in the
16:
    cycle.
             else
17:
                 if s_{i+1,n} = s_{0.n} then
                     m \leftarrow 1 #If the cycle ends return the count of phases m back to 1
19:
                 return s_{i+1,n} and m #Actuate the next phase in the sequence
             end if
        end if
24: end procedure
```

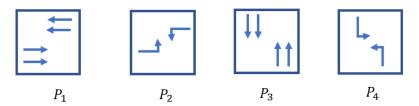
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Case study: 3x3 Grid Network Results

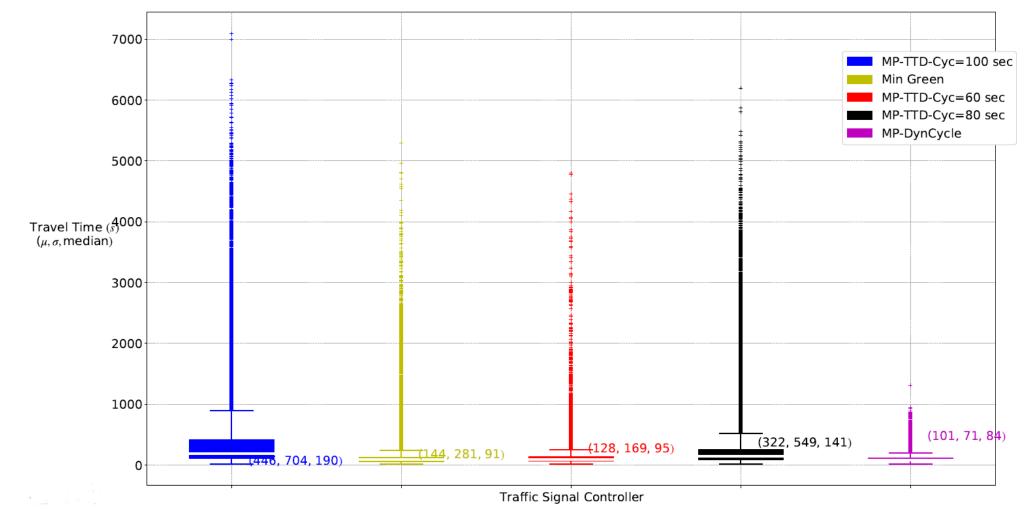




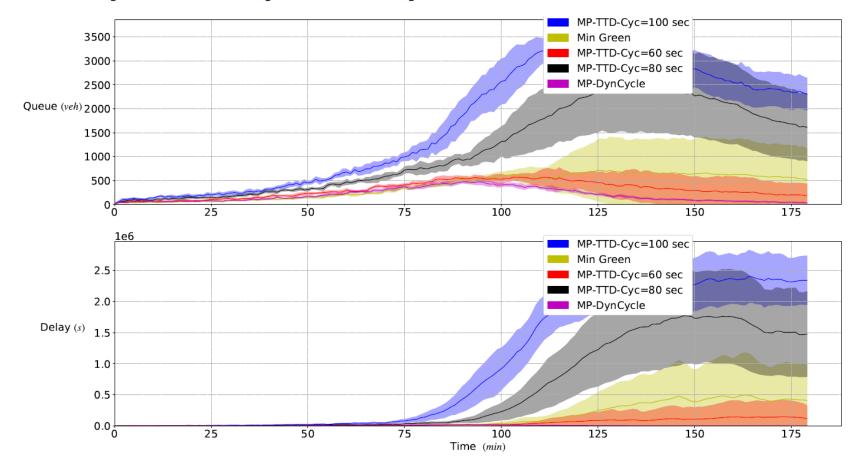
Adaptive Traffic Signal Control: Principles and Applications of Max-Pressure

MP-TTD: fixed cycle vs. dynamic (unbounded) cycle

• different fixed cycles (60, 80, 100) vs. dynamic cycle.



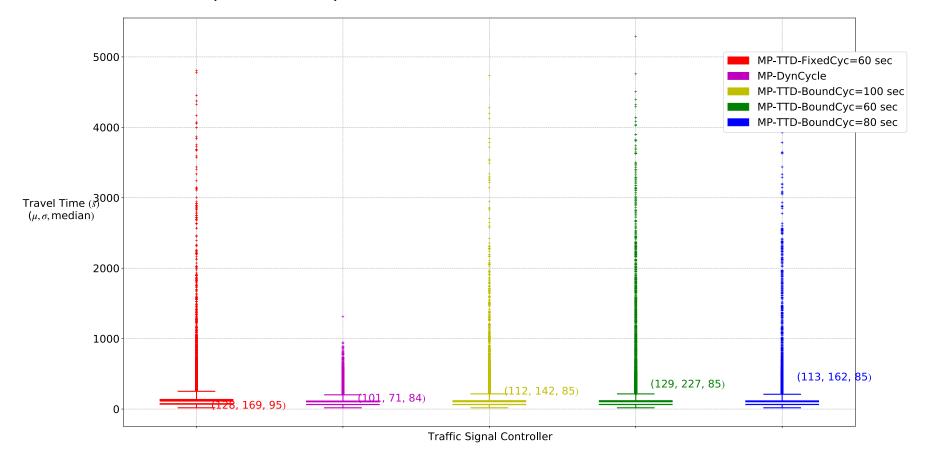
MP-TTD: fixed cycle vs. dynamic cycle



• dynamic cycle provides superior performance compared with fixed cycle MP.

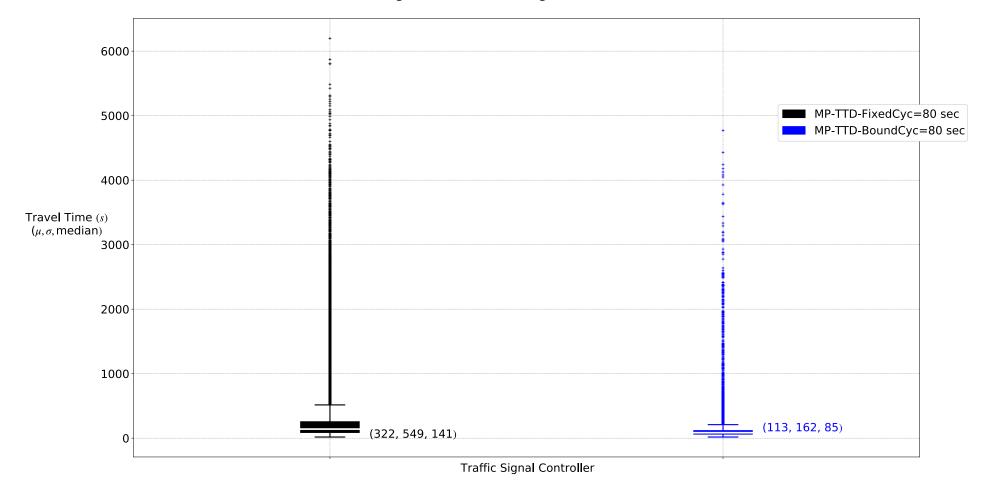
MP-TTD: Bounded vs. unbounded dynamic cycle

• different **bounded** cycles (60, 80, 100) vs. dynamic cycle.



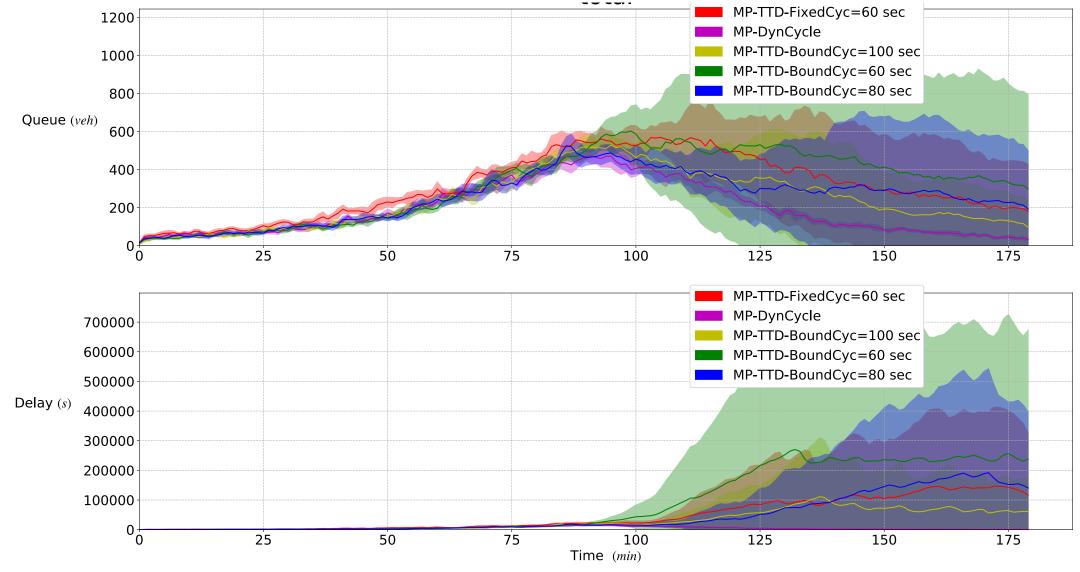
• The less algorithm is bounded the more stable and less performance variation.

MP-TTD: Fixed vs. bounded dynamic cycle



• A bounded dynamic cycle (maximum cycle 80s) algorithm can perform better than a fixed cycle (80s) scheme.

MP-TTD: Bounded vs. unbounded dynamic cycle



Summary of simulation results

- Choosing appropriate fixed cycle is vital to ensure better utilization of the cyclic MP controller.
- The developed dynamic cyclic MP algorithm can manage to surpass other existing fixed cyclic MP schemes, providing better coordination and better green allocations, both result in better performances.
- The less bounded dynamic cycle is the more stable and less performance variation, and it performs better than the existing fixed cycle scheme.

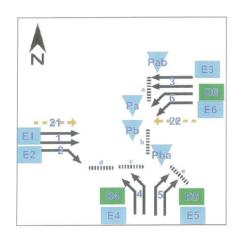
Outline

- 1 Introduction
- 2 Background
- 3 Fixed cyclic MP

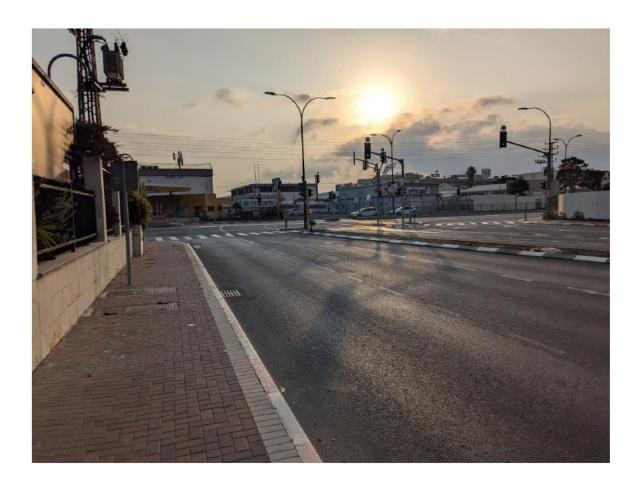
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Experimental case study



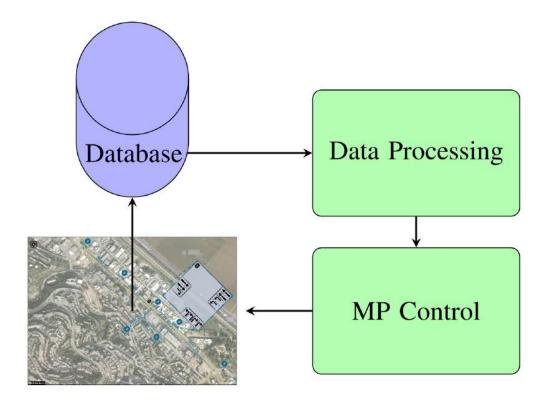






Communication architecture

- Bluetooth Sensor Database: This component serves as the central repository where data from Bluetooth sensors is collected and stored.
- Data Processing: In this stage, the raw data collected from the sensors is processed to prepare it for further subsequent analysis.
- MP Control: Here, the processed data is analyzed using the MP-TTD algorithm, performing adaptive algorithm calculations.
- Environment Activation: Based on the results from the MP-TTD calculations, the system adjusts the green time durations, directly interacting with the traffic signals in the real-world environment.

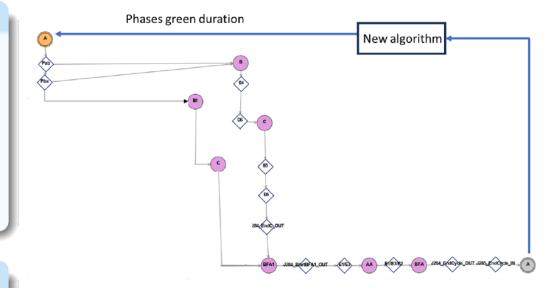


Constraints

- Same Flow chart: adapt to the same flow chart, without loop detectors.
- Fixed cycle time & effective green: no change for the cycle.
- **Pedestrian green wave** : pedestrian cross without stopping.

Challenges of Data collection

- **Feedback delay**: the control is activated in large delay.
- low penetration rate: 5-10% penetration rate.
- **Data Filtering**: difficult to filter with high variations.



Experimental case study:Data collection

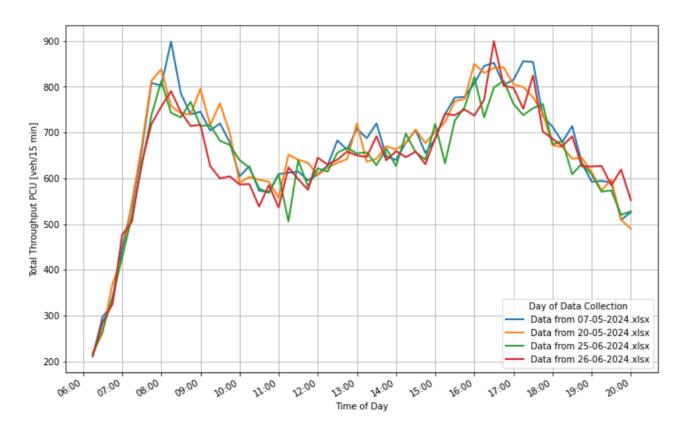


Figure: Use case Total throughput Passenger car unit over Time Intervals by Data Collection Day

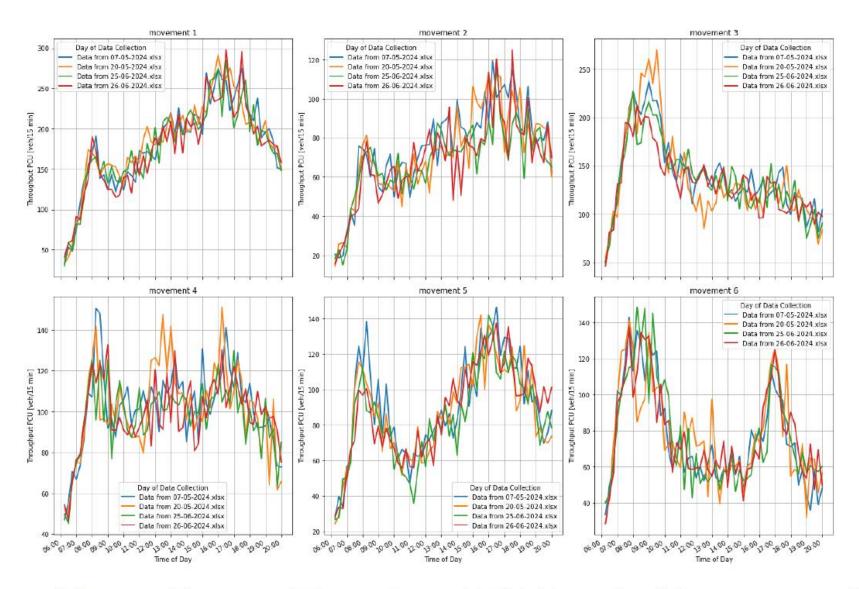
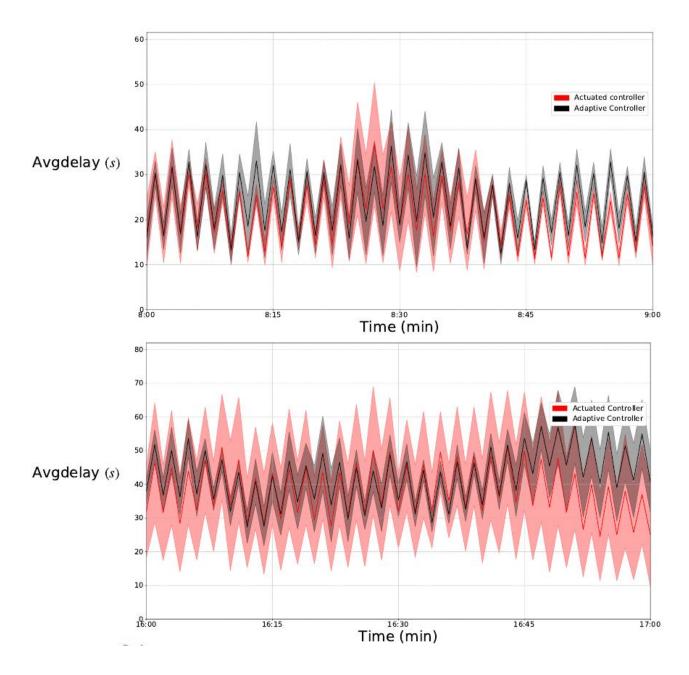
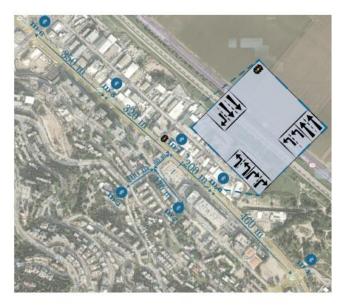


Figure: Use case Throughput PCU Data by Movement and Day



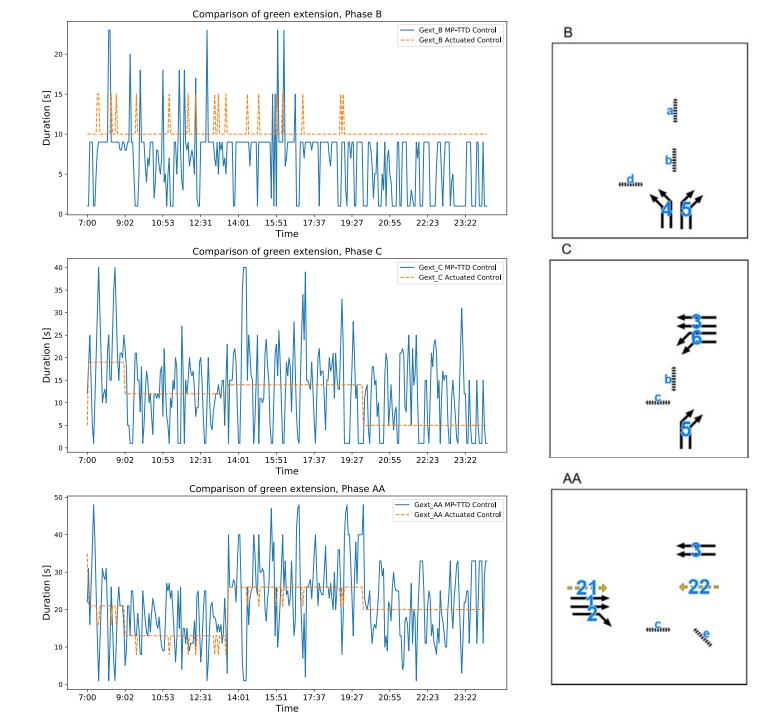


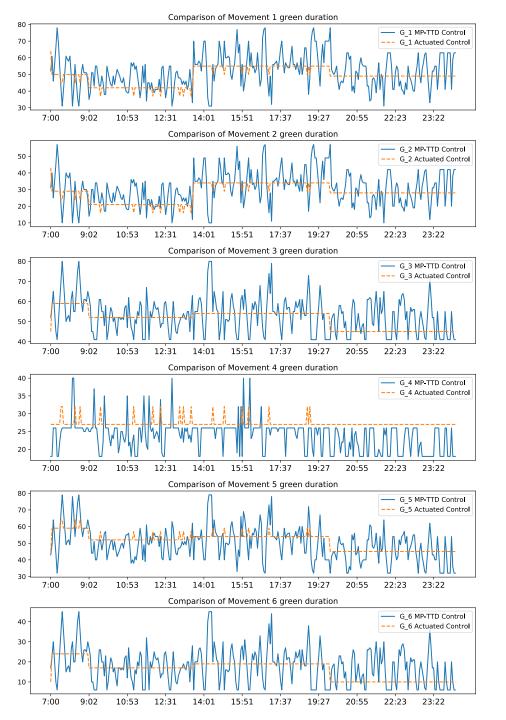


Experimental case study:Field Test

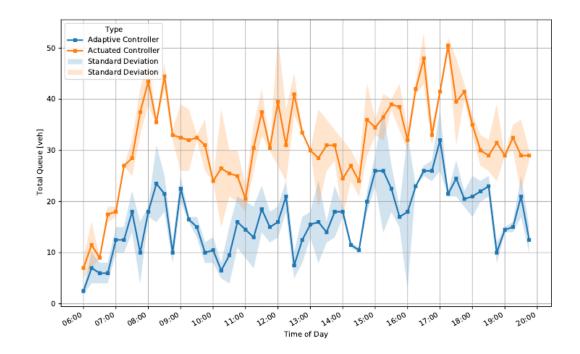


Experimental case study: Activation results





Experimental case study:Performance results



The data reveals a 47.5% queue improvement with the adaptive controller over the actuated control from 07:00 to 20:00.

Experimental case study:Performance results

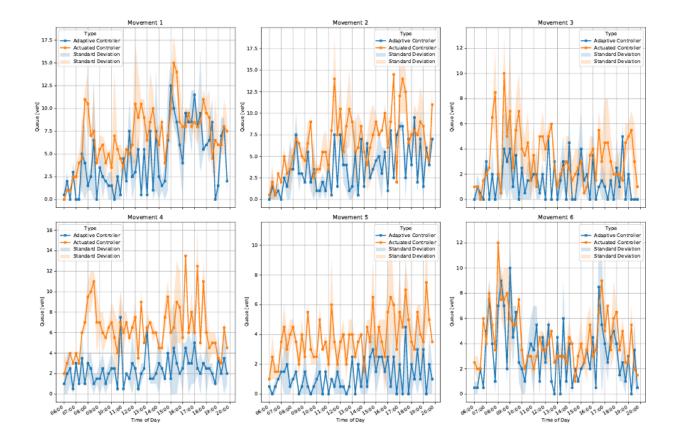


Figure: Experimental case study results: Queue per movement throughout the day from 7:00 to 20:00.

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Conclusions

- The developed MP-TTD controller can manage surpass other existing max pressure schemes, providing an enhanced estimation of the traffic state and an improved green allocation, both result in better performance.
- The adaptive signal control algorithm, through experimental application, demonstrated potential for enhancing traffic flow.
- in a practical experimental case study using real-time data from Bluetooth sensors, the MP-TTD controller was integrated with existing traffic signal systems without requiring major infrastructure changes.
- the MP-TTD controller shows promise as a tool for improving urban traffic signal control. Its real-world efficacy and adaptability suggest it could be beneficial for urban and possibly rural settings.